

# Microwave Spectra of Dimethylether (CH<sub>3</sub>)<sub>2</sub>O and (CD<sub>3</sub>)<sub>2</sub>O in Excited Torsional States

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*Dedicated to Yonezo Morino*

The rotational spectra of the torsional excited states  $\tilde{\nu}_n = 1_1, 1_2, 2_1, 2_2, 2_3$  have been measured and assigned. The torsional fine structure was used to determine the coefficients  $V_3$  and  $V'_{12}$  of the hindering potential.

For (CH<sub>3</sub>)<sub>2</sub>O:  $V_3 = 2618 \pm 4$  cal/mole,  $V'_{12} = 18 \pm 8$  cal/mole, for (CD<sub>3</sub>)<sub>2</sub>O:  $V_3 = 2572 \pm 6$  cal/mole,  $V'_{12} = 29 \pm 12$  cal/mole,  $V_{12}$  was correlated to  $V_3$ .

## Introduction

Dimethylether was one of the first molecules [1] with two methyl tops (two top molecule) investigated by microwave spectroscopy for the determination of the barrier to internal rotation. Usually the hindering potential is described by a two dimensional Fourier series in the torsional angles  $\alpha_i$ ,  $i = 1, 2$ . For molecules with two equivalent tops and  $C_{2v}$ -symmetry it may be given in the form:

$$V(\alpha_1, \alpha_2) = \frac{V_3}{2} (1 - \cos 3\alpha_1) + \frac{V_3}{2} (1 - \cos 3\alpha_2) + V'_{12} \sin 3\alpha_1 \sin 3\alpha_2 + V_{12} \cos 3\alpha_1 \cos 3\alpha_2 + \dots \quad (1)$$

$V_3$  is the hindering potential,  $V'_{12}$  and  $V_{12}$  are top-top coupling parameters. The analysis of the rotational spectra is based on a rigid frame rigid top Hamiltonian, which was discussed in detail elsewhere [2–8] and is given later under Equation (2).

This Hamiltonian allows for two internal degrees of freedom, the methyltorsions, and three degrees of freedom for the overall rotation. All other vibrational degrees of freedom are excluded.

By the analysis of the rotational spectrum in the ground-state,  $V_3$  was determined [1, 9]. As in similar cases [10, 11] the top-top coupling coefficient  $V'_{12}$  can only be determined, if the rotational spectra of the excited torsional states  $\tilde{\nu}_n = 1_1$  and  $1_2^{**}$  are analysed. For Dimethylether this was done independently by [12–14].  $V_{12}$  could not be determined, as it was correlated to  $V_3$  as noticed in similar work

[11]. This correlation may be seen, if the harmonic approximation is calculated.

$$V(\alpha_1, \alpha_2) \approx \frac{9}{4} (V_3 - 2 V_{12}) (\alpha_1^2 + \alpha_2^2) + 9 V'_{12} \alpha_1 \alpha_2. \quad (1a)$$

$V_3$  and  $V_{12}$  are combined in the coefficient of  $\alpha_1^2 + \alpha_2^2$ . Our investigation presented in this paper was initiated to determine the top-top coupling coefficient  $V_{12}$  [see Eq. (1)] from the rotational spectra of the torsional excited states  $\tilde{\nu}_n = 2_1, 2_2, 2_3$ , as a consideration of the Hamiltonian showed that at least these spectra should be included in the analysis. As the  $2_n$ -states are near to half the barrier height  $V_3$ , we believed, that (1a) is no more a good approximation. But it proved finally, that  $V_{12}$  is still correlated to  $V_3$ . Nevertheless we like to give the results as to our knowledge a detailed analysis of rotational spectra of the torsional excited states  $\tilde{\nu}_n = 2_1, 2_2, 2_3$  for a two top molecule is not yet published. Our analysis is applied to the two isotopic forms (CH<sub>3</sub>)<sub>2</sub>O and (CD<sub>3</sub>)<sub>2</sub>O.

## Experimental

The spectra of (CH<sub>3</sub>)<sub>2</sub>O and (CD<sub>3</sub>)<sub>2</sub>O were recorded in the region from 8 to 40 GHz by a conventional Stark spectrometer [15, 16] equipped with an 8 m absorption cell and employing 33 kHz Stark square wave modulation. The sample pressure was 10 mT and the temperature was kept between 0 °C and –50 °C. For the assignment of the lines in the higher torsional states microwave-microwave double resonance (MW-MW-DR) experiments proved very useful. The MW-MW-DR-Spectrometer is described in detail in [17]. (CD<sub>3</sub>)<sub>2</sub>O was supplied by Isocommerz GmbH Leipzig.

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\*\* For the labelling of the levels see [11].

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### Measurement and Assignment of the Spectra \*

For the assignment of the spectra we used the following criteria:

- Stark effect;
- Relative spin weights [6, 7];
- Boltzmann factors of the different states;
- Fit of the A<sub>i</sub>A<sub>j</sub>- and A<sub>i</sub>E-rotational lines to a rigid rotor spectrum;
- Similarities of the frequency shifts with respect to the ground state of the Q-series  $J_{0J} - J_{1,J-1}$ ,  $\tilde{\nu}_n$  for (CD<sub>3</sub>)<sub>2</sub>O and (CH<sub>3</sub>)<sub>2</sub>O;
- Double resonances;
- Theoretical predictions of the internal rotation splittings.

As especially the assignment of the rotational spectra in the 2<sub>n</sub>-torsional states was difficult, the combination of all the mentioned criteria was necessary.

As the internal rotation splittings are smaller for (CD<sub>3</sub>)<sub>2</sub>O we tried to assign this isotopic species first\*\*. The unsplit ground state,  $\tilde{\nu}_n = 0_1$ -spectrum had been assigned earlier [19]. The reported lines were measured with higher precision. These and some additionally measured lines are given in Table 1. The lines up to  $J = 3$  were fitted by a rigid rotor spectrum. The rotational constants are given in Table 4.

The low  $J$ -lines of the states  $\tilde{\nu}_n = 1_1$  and  $1_2$  were found within a frequency region of  $\pm 300$  MHz of the respective ground state lines. They were assigned by the mentioned criteria a)–d). The low  $J$ -lines of the states  $\tilde{\nu}_n = 2_1, 2_2$  and  $2_3$  were located in a  $\pm 400$  MHz region. The assignment was

\* For the group theoretical labelling see [6], [7].

\*\* For more details see Ref. [18].

possible by application of the criteria a)–d) and g). The measured lines are given in Tables 2 and 3. Table 4 summarises the effective A<sub>i</sub>A<sub>j</sub>- and A<sub>i</sub>E-rotational constants.

Figures 1 and 2 illustrate the frequency shifts with respect to the ground state lines of the  $J_{0,J} - J_{1,J-1}$ ,  $\tilde{\nu}_n$ -series. The regularity within one series is an additional indication for the validity of the assignment.

For (CH<sub>3</sub>)<sub>2</sub>O the ground state spectrum had been assigned earlier [1, 19]. Additional measurements for astrophysical reasons were made recently [20].

The assignment of the rotational lines of the torsional states  $\tilde{\nu}_n = 1_1$  and  $1_2$  was successful first for the  $J_{0,J} - J_{1,J-1}$ ,  $1_n$ -series by the criterion e), which is illustrated in Fig. 1, in combination with criteria a), b) and g). The assignment of an additional  $\Delta J = 1$ -line for each  $1_n$ -state concluded the assignment. The consistency was checked with criterion d).

For the 2<sub>n</sub>-state spectra the assignment proved to be rather difficult, as the lines are weak and the torsional multiplets are split by about 1 GHz. As a consequence of the large splittings the three 2<sub>n</sub>-multiplets are mixed in their order.

The criteria b) and c) cannot be applied as the intensity cannot be determined reliably with our spectrometer for largely splitted multiplets, as the microwave power fluctuates with frequency.

The assignment was guided by the hints given by the similarities of the (CD<sub>3</sub>)<sub>2</sub>O- and (CH<sub>3</sub>)<sub>2</sub>O-spectra [criterion e)] as illustrated in Figure 2. By using the Stark-effect the A<sub>i</sub>A<sub>j</sub>-components of the  $J_{0,J} - J_{1,J-1}$ , 2<sub>n</sub>-series could be assigned. The EE-components were identified by the Stark-effect, which contains linear contributions, and by application of criterion g) with data gained by the analysis of the 1<sub>n</sub>-state spectra. Criterion g) and a)

Table 1. Rotational lines of (CD<sub>3</sub>)<sub>2</sub>O for the  $\tilde{\nu}_n = 0_1$  torsional state [MHz].

| $J_{K-K+} - J'_{K'-K+}$           | $\nu_{\text{exp}}$    | $J_{K-K+} - J'_{K'-K+}$           | $\nu_{\text{exp}}$    | $J_{K-K+} - J'_{K'-K+}$               | $\nu_{\text{exp}}$ |
|-----------------------------------|-----------------------|-----------------------------------|-----------------------|---------------------------------------|--------------------|
| 0 <sub>00</sub> – 1 <sub>11</sub> | 32494.43 <sup>a</sup> | 4 <sub>04</sub> – 4 <sub>13</sub> | 22216.85 <sup>a</sup> | 6 <sub>24</sub> – 7 <sub>17</sub>     | 33036.44           |
| 1 <sub>01</sub> – 1 <sub>10</sub> | 18898.26 <sup>a</sup> | 4 <sub>23</sub> – 5 <sub>14</sub> | 20761.65              | 7 <sub>07</sub> – 7 <sub>16</sub>     | 29911.81           |
| 1 <sub>11</sub> – 2 <sub>02</sub> | 10332.22 <sup>a</sup> | 5 <sub>24</sub> – 4 <sub>31</sub> | 21473.52              | 7 <sub>35</sub> – 8 <sub>26</sub>     | 24418.83           |
| 2 <sub>02</sub> – 2 <sub>11</sub> | 19603.00 <sup>a</sup> | 4 <sub>22</sub> – 5 <sub>15</sub> | 10201.72              | 7 <sub>34</sub> – 8 <sub>27</sub>     | 20538.52           |
| 2 <sub>12</sub> – 3 <sub>03</sub> | 25223.63 <sup>a</sup> | 5 <sub>23</sub> – 4 <sub>32</sub> | 20811.53              | 12 <sub>58</sub> – 13 <sub>49</sub>   | 19721.10           |
| 3 <sub>12</sub> – 2 <sub>21</sub> | 10774.87              | 5 <sub>05</sub> – 5 <sub>14</sub> | 24219.84 <sup>a</sup> | 12 <sub>57</sub> – 13 <sub>4,10</sub> | 19607.15           |
| 3 <sub>13</sub> – 2 <sub>20</sub> | 14907.89              | 5 <sub>23</sub> – 6 <sub>16</sub> | 21948.94              |                                       |                    |
| 3 <sub>03</sub> – 3 <sub>12</sub> | 20695.42 <sup>a</sup> | 5 <sub>24</sub> – 6 <sub>15</sub> | 36979.37              |                                       |                    |

<sup>a</sup> Measured by Blukis et al. [19].

Table 2. Rotational lines of (CD<sub>3</sub>)<sub>2</sub>O for the  $\tilde{\nu}_n = 1_1$  and  $1_2$  torsional states [MHz].

| $J_{K-}K_+$<br>— $J_{K'-}K_+'$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ | $J_{K-}K_+$<br>— $J_{K'-}K_+'$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ |
|--------------------------------|---------------------------------------------------|--------------------|---------------------------|---------------------------|----------------------------------------------------------|--------------------------------|---------------------------------------------------|--------------------|---------------------------|---------------------------|----------------------------------------------------------|
| $0_{00} \rightarrow 1_{11}$    | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 32487.62           |                           |                           |                                                          | $3_{12} - 2_{21}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 10936.10           |                           |                           |                                                          |
|                                |                                                   | 32487.88           | 0.25                      | 0.25                      | 0.00                                                     |                                |                                                   | 10936.70           | 0.60                      | 0.65                      | -0.05                                                    |
|                                |                                                   | 32488.13           | 0.51                      | 0.46                      | 0.05                                                     |                                |                                                   | 10937.35           | 1.25                      | 1.23                      | 0.02                                                     |
|                                |                                                   |                    |                           | 0.47                      | 0.04                                                     |                                |                                                   | 10937.25           | 1.15                      | 1.28                      | -0.13                                                    |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 32468.75           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 10978.92           |                           |                           |                                                          |
|                                |                                                   | 32468.99           | 0.24                      | 0.22                      | 0.02                                                     |                                |                                                   | 10979.48           | 0.56                      | 0.56                      | 0.00                                                     |
|                                |                                                   | 32469.23           | 0.48                      | 0.38                      | 0.10                                                     |                                |                                                   | 10980.00           | 1.17                      | 1.03                      | 0.14                                                     |
|                                |                                                   |                    |                           | 0.40                      | 0.08                                                     |                                |                                                   | 10980.09           | 1.08                      | 0.96                      | 0.12                                                     |
| $1_{01} \rightarrow 1_{10}$    | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 18916.15           |                           |                           |                                                          | $4_{04} - 4_{13}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 22211.34           |                           |                           |                                                          |
|                                |                                                   | 18916.41           | 0.27                      | 0.25                      | 0.02                                                     |                                |                                                   | 22211.62           | 0.29                      | 0.30                      | -0.01                                                    |
|                                |                                                   | 18916.66           | 0.51                      | 0.46                      | 0.05                                                     |                                |                                                   | 22211.91           | 0.57                      | 0.55                      | 0.02                                                     |
|                                |                                                   |                    |                           | 0.47                      | 0.04                                                     |                                |                                                   |                    |                           | 0.57                      | 0.00                                                     |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 18881.13           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 22041.16           |                           |                           |                                                          |
|                                |                                                   | 18881.40           | 0.25                      | 0.22                      | 0.03                                                     |                                |                                                   | 22041.43           | 0.27                      | 0.25                      | 0.02                                                     |
|                                |                                                   | 18881.64           | 0.51                      | 0.38                      | 0.13                                                     |                                |                                                   | 22041.69           | 0.54                      | 0.45                      | 0.09                                                     |
|                                |                                                   |                    |                           | 0.40                      | 0.11                                                     |                                |                                                   |                    |                           | 0.47                      | 0.07                                                     |
| $1_{11} \rightarrow 2_{02}$    | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 10251.78           |                           |                           |                                                          | $4_{23} - 5_{14}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 20523.60           |                           |                           |                                                          |
|                                |                                                   | 10251.55           | -0.23                     | -0.22                     | -0.01                                                    |                                |                                                   | 20523.03           | -0.57                     | -0.59                     | 0.02                                                     |
|                                |                                                   | 10251.33           | -0.45                     | -0.41                     | -0.04                                                    |                                |                                                   | 20522.46           | -1.14                     | -1.12                     | -0.02                                                    |
|                                |                                                   |                    |                           | -0.42                     | -0.03                                                    |                                |                                                   |                    |                           | -1.16                     | 0.02                                                     |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 10241.59           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 20350.59           |                           |                           |                                                          |
|                                |                                                   | 10241.40           | -0.19                     | -0.19                     | 0.00                                                     |                                |                                                   | 20350.06           | -0.53                     | -0.54                     | 0.01                                                     |
|                                |                                                   | 10241.19           | -0.40                     | -0.34                     | -0.06                                                    |                                |                                                   | 20349.53           | -1.06                     | -0.94                     | -0.12                                                    |
|                                |                                                   |                    |                           | -0.36                     | -0.04                                                    |                                |                                                   |                    |                           |                           |                                                          |
| $2_{02} - 2_{11}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 19616.14           |                           |                           |                                                          | $5_{23} - 6_{16}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 21772.55           |                           |                           |                                                          |
|                                |                                                   | 19616.40           | 0.26                      | 0.26                      | 0.00                                                     |                                |                                                   | 21771.85           | -0.69                     | -0.79                     | 0.10                                                     |
|                                |                                                   | 19616.67           | 0.53                      | 0.48                      | 0.05                                                     |                                |                                                   | 21771.16           | -1.39                     | -1.46                     | 0.07                                                     |
|                                |                                                   |                    |                           | 0.49                      | 0.04                                                     |                                |                                                   |                    |                           | -1.52                     | 0.13                                                     |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 19553.49           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 22116.45           |                           |                           |                                                          |
|                                |                                                   | 19553.74           | 0.25                      | 0.22                      | 0.03                                                     |                                |                                                   | 22115.80           | -0.65                     | -0.68                     | 0.03                                                     |
|                                |                                                   | 19553.74           | 0.50                      | 0.39                      | 0.11                                                     |                                |                                                   | 22115.15           | -1.29                     | -1.20                     | -0.09                                                    |
|                                |                                                   |                    |                           | 0.42                      | 0.08                                                     |                                |                                                   |                    |                           | -1.27                     | -0.02                                                    |
| $3_{03} - 3_{12}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 20700.95           |                           |                           |                                                          | $5_{05} - 5_{14}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 24199.16           |                           |                           |                                                          |
|                                |                                                   | 20701.22           | 0.27                      | 0.27                      | 0.00                                                     |                                |                                                   | 24199.47           | 0.31                      | 0.33                      | -0.02                                                    |
|                                |                                                   | 20701.49           | 0.55                      | 0.51                      | 0.04                                                     |                                |                                                   | 24199.77           | 0.61                      | 0.61                      | 0.00                                                     |
|                                |                                                   |                    |                           | 0.53                      | 0.02                                                     |                                |                                                   |                    |                           | 0.63                      | -0.02                                                    |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 20594.22           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 23942.48           |                           |                           |                                                          |
|                                |                                                   | 20594.48           | 0.26                      | 0.24                      | 0.02                                                     |                                |                                                   | 23942.76           | 0.28                      | 0.27                      | 0.01                                                     |
|                                |                                                   | 20594.74           | 0.51                      | 0.42                      | 0.09                                                     |                                |                                                   | 23943.05           | 0.56                      | 0.49                      | 0.07                                                     |
|                                |                                                   |                    |                           | 0.44                      | 0.07                                                     |                                |                                                   |                    |                           | 0.51                      | 0.05                                                     |
| $3_{13} - 2_{20}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 15042.03           |                           |                           |                                                          | $4_{22} - 5_{15}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 10034.51           |                           |                           |                                                          |
|                                |                                                   | 15042.75           | 0.72                      | 0.73                      | -0.01                                                    |                                |                                                   | 10033.82           | -0.69                     | -0.76                     | 0.07                                                     |
|                                |                                                   | 15043.48           | 1.45                      | 1.36                      | 0.09                                                     |                                |                                                   | 10033.13           | -1.38                     | -1.41                     | 0.03                                                     |
|                                |                                                   |                    |                           | 1.40                      | 0.05                                                     |                                |                                                   |                    |                           | -1.46                     | 0.08                                                     |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | -                  |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 10275.29           |                           |                           |                                                          |
|                                |                                                   | -                  |                           | 0.67                      |                                                          |                                |                                                   | 10274.66           | -0.63                     | -0.66                     | 0.03                                                     |
|                                |                                                   | -                  |                           | 1.12                      |                                                          |                                |                                                   | 10274.03           | -1.26                     | -1.16                     | -0.10                                                    |
|                                |                                                   | -                  |                           | 1.31                      |                                                          |                                |                                                   |                    |                           | -1.24                     | -0.02                                                    |
| $2_{12} - 3_{03}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 25110.64           |                           |                           |                                                          | $5_{24} - 4_{31}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 21718.98           |                           |                           |                                                          |
|                                |                                                   | 25110.40           | -0.24                     | -0.20                     | -0.04                                                    |                                |                                                   | 21720.11           | 1.13                      | 1.23                      | -0.10                                                    |
|                                |                                                   | 25110.19           | -0.45                     | -0.31                     | -0.14                                                    |                                |                                                   | 21720.65           | 1.67                      | 2.25                      | -0.58                                                    |
|                                |                                                   |                    |                           | -0.38                     | -0.07                                                    |                                |                                                   | 21721.56           | 2.58                      | 2.30                      | 0.28                                                     |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 25069.61           |                           |                           |                                                          |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 21652.63           |                           |                           |                                                          |
|                                |                                                   | 25069.40           | -0.20                     | -0.18                     | -0.02                                                    |                                |                                                   | 21653.71           | 1.09                      | 1.50                      | -0.41                                                    |
|                                |                                                   | 25069.20           | -0.41                     | -0.37                     | -0.04                                                    |                                |                                                   | 21654.22           | 1.59                      | 1.83                      | -0.14                                                    |
|                                |                                                   |                    |                           | -0.33                     | -0.08                                                    |                                |                                                   | 21655.12           | 2.49                      | 3.36                      | -0.87                                                    |

Table 2 (continued).

| $J_{K-K_+}$<br>$-J_{K'-K'_+}$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>$-\Delta \nu_{\text{cal}}$ | $J_{K-K_+}$<br>$-J_{K'-K'_+}$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>$-\Delta \nu_{\text{cal}}$ |
|-------------------------------|---------------------------------------------------|--------------------|---------------------------|---------------------------|---------------------------------------------------------|-------------------------------|---------------------------------------------------|--------------------|---------------------------|---------------------------|---------------------------------------------------------|
| $6_{06} - 6_{15}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 26723.69           |                           |                           |                                                         | $6_{24} - 7_{17}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 32857.32           |                           |                           |                                                         |
|                               |                                                   | 26724.01           | 0.32                      | 0.37                      | -0.05                                                   |                               |                                                   | 32856.58           | -0.74                     | -0.83                     | 0.09                                                    |
|                               |                                                   | 26724.34           | 0.65                      | 0.68                      | -0.03                                                   |                               |                                                   | 32855.88           | -1.44                     | -1.54                     | 0.10                                                    |
|                               |                                                   |                    |                           | 0.70                      | -0.05                                                   |                               |                                                   |                    |                           | -1.58                     | 0.14                                                    |
|                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 26353.66           |                           |                           |                                                         |                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 33339.64           |                           |                           |                                                         |
|                               |                                                   | 26353.95           | 0.29                      | 0.30                      | -0.01                                                   |                               |                                                   | 33339.00           | -0.64                     | -0.71                     | 0.07                                                    |
|                               |                                                   | 26354.25           | 0.59                      | 0.55                      | 0.04                                                    |                               |                                                   | 33338.34           | -1.30                     | -1.26                     | -0.04                                                   |
|                               |                                                   |                    |                           | 0.57                      | 0.02                                                    |                               |                                                   |                    |                           | -1.32                     | 0.02                                                    |
| $7_{07} - 7_{16}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 29845.76           |                           |                           |                                                         | $7_{34} - 8_{27}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 20217.50           |                           |                           |                                                         |
|                               |                                                   | 29846.11           | 0.35                      | 0.43                      | -0.08                                                   |                               |                                                   | 20216.73           | -0.77                     |                           |                                                         |
|                               |                                                   | 29846.45           | 0.69                      | 0.76                      | -0.07                                                   |                               |                                                   | 20215.96           | -1.54                     |                           |                                                         |
|                               |                                                   |                    |                           | 0.80                      | -0.11                                                   |                               |                                                   |                    |                           |                           |                                                         |
|                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 29332.25           |                           |                           |                                                         |                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 20315.31           |                           |                           |                                                         |
|                               |                                                   | 29332.57           | 0.32                      | 0.33                      | -0.01                                                   |                               |                                                   | 20314.59           | -0.72                     |                           |                                                         |
|                               |                                                   | 29332.85           | 0.64                      | 0.61                      | 0.03                                                    |                               |                                                   | 20313.87           | -1.45                     |                           |                                                         |
|                               |                                                   |                    |                           | 0.64                      | 0.00                                                    |                               |                                                   |                    |                           |                           |                                                         |
| $5_{24} - 6_{15}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 36700.52           |                           |                           |                                                         | $7_{35} - 8_{26}$             | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 24045.41           |                           |                           |                                                         |
|                               |                                                   | 36699.99           | -0.53                     | -0.55                     | 0.02                                                    |                               |                                                   | 24044.68           | -0.73                     |                           |                                                         |
|                               |                                                   | 36699.47           | -1.05                     | -1.05                     | 0.00                                                    |                               |                                                   | 24043.95           | -1.47                     |                           |                                                         |
|                               |                                                   |                    |                           | -1.08                     | 0.03                                                    |                               |                                                   |                    |                           |                           |                                                         |
|                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 36447.68           |                           |                           |                                                         |                               | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 23866.33           |                           |                           |                                                         |
|                               |                                                   | 36447.17           | -0.51                     | -0.52                     | 0.01                                                    |                               |                                                   | 23865.64           | 0.69                      |                           |                                                         |
|                               |                                                   | 36446.68           | -1.01                     | -0.89                     | -0.12                                                   |                               |                                                   | 23864.96           | 1.37                      |                           |                                                         |
|                               |                                                   |                    |                           | -0.94                     | -0.07                                                   |                               |                                                   |                    |                           |                           |                                                         |

in combination were also necessary to assign the EA<sub>i</sub>-components. For the A<sub>i</sub>E-components it was necessary to record the spectra with low Stark field (20–200 V/cm) as they have a strong linear contribution to the Stark effect. At higher voltages they are broadened or smeared out, as the basis of the Stark square wave is not ideally zeroed and the Stark field is inhomogeneous.

The multiplets of the  $\Delta J=1$  line  $2_{02}-1_{11}$  were located by MW-MW-DR experiments. To connect the line with the assigned line  $2_{02}-2_{11}$  we kept the signal source fixed to the components of the  $2_{02}-2_{11}$  line and swept the pump. Initial searches were made over 3 GHz with unstabilised pump sources. A sweep over 1.5 GHz is shown in Figure 3. The roughly determined frequencies were refined by stabilised sweeps of the pump source and by measurements with the Stark spectrometer.

The measured spectra are given in Tables 5–7. In Table 8 the A<sub>i</sub>A<sub>j</sub>- and A<sub>i</sub>E-rotational constants are listed.

### Analysis of the Torsional Splittings

The analysis is based on the rigid frame-rigid top model. The Hamiltonian is given in Eq. (2):

$$\begin{aligned}
 \mathcal{H} = & AP_a^2 + BP_b^2 + CP_c^2 + F_1 \mathcal{P}_1^2 + F_2 \mathcal{P}_2^2 \\
 & + F'(\mathcal{P}_1 \mathcal{P}_2 + \mathcal{P}_2 \mathcal{P}_1) + F_1 p_1^2 \\
 & + \frac{V_3}{2}(1 - \cos 3\alpha_1) + F_2 p_2^2 \\
 & + \frac{V_3}{2}(1 - \cos 3\alpha_2) + F'(p_1 p_2 + p_2 p_1) \\
 & + V_{12} \cos 3\alpha_1 \cos 3\alpha_2 + V'_{12} \sin 3\alpha_1 \sin 3\alpha_2 \\
 & - F'(p_1 \mathcal{P}_2 + p_2 \mathcal{P}_1) - 2F_1 p_1 \mathcal{P}_1 - 2F_2 p_2 \mathcal{P}_2;
 \end{aligned} \tag{2}$$

$A, B, C$  rotational constants,

$g = a, b, c$  indices label molecule fixed principal inertia axes,

$I_g$  principal moments of inertia,

$I_\alpha$  moment of inertia of the tops about their symmetry axis,

Table 3. Rotational lines of (CD<sub>3</sub>)<sub>2</sub>O for the  $\bar{\nu}_n = 2_1, 2_2$  and  $2_3$  torsional state [MHz] for  $\bar{\nu}_n = 2_1$  and  $2_3$ : A<sub>1</sub>A<sub>1</sub>, EE, A<sub>1</sub>E, EA<sub>1</sub>, for  $\bar{\nu}_n = 2_2$ : A<sub>2</sub>A<sub>2</sub>, EE, A<sub>2</sub>E, EA<sub>2</sub>.

| $J_{K-K+}$<br>— $J_{K'-K+}$ | $\bar{\nu}_n \Gamma \Gamma' v_{\text{exp}}$                    | $\Delta v_{\text{exp}}$ | $\Delta v_{\text{cal}}$ | $\Delta v_{\text{exp}}$<br>— $\Delta v_{\text{cal}}$ | $J_{K-K+}$<br>— $J_{K'-K+}$ | $\bar{\nu}_n \Gamma \Gamma' v_{\text{exp}}$                    | $\Delta v_{\text{exp}}$ | $\Delta v_{\text{cal}}$ | $\Delta v_{\text{exp}}$<br>— $\Delta v_{\text{cal}}$ |
|-----------------------------|----------------------------------------------------------------|-------------------------|-------------------------|------------------------------------------------------|-----------------------------|----------------------------------------------------------------|-------------------------|-------------------------|------------------------------------------------------|
| $0_{00} - 1_{11}$           | $2_1$ AA 32496.44<br>EE 32491.43<br>AE 32486.66<br>EA 32486.16 |                         |                         |                                                      | $3_{03} - 3_{12}$           | $2_1$ AA 20721.48<br>EE 20716.36<br>AE 20711.23<br>EA          |                         |                         |                                                      |
|                             |                                                                | -5.01                   | -5.16                   | 0.15                                                 |                             |                                                                | -5.13                   | -5.38                   | 0.25                                                 |
|                             |                                                                | -9.78                   | -9.95                   | 0.17                                                 |                             |                                                                | -10.25                  | -10.82                  | 0.57                                                 |
|                             |                                                                | -10.28                  | -10.71                  | 0.42                                                 |                             |                                                                | -10.25                  | -10.72                  | 0.47                                                 |
|                             | $2_2$ AA 32474.24<br>EE 32465.31<br>AE 32457.19<br>EA 32455.59 |                         |                         |                                                      |                             | $2_2$ AA 20639.29<br>EE 20630.41<br>AE 20621.42<br>EA 20621.61 |                         |                         |                                                      |
|                             |                                                                | -8.94                   | -8.62                   | -0.32                                                |                             |                                                                | -8.88                   | -8.90                   | 0.02                                                 |
|                             |                                                                | -17.06                  | -16.41                  | -0.64                                                |                             |                                                                | -17.87                  | -17.98                  | 0.11                                                 |
|                             |                                                                | -18.65                  | -18.18                  | -0.48                                                |                             |                                                                | -17.67                  | -17.77                  | 0.10                                                 |
|                             | $2_3$ AA 32512.29<br>EE 32509.32<br>AE 32506.52<br>EA          |                         |                         |                                                      |                             | $2_3$ AA 20626.77<br>EE 20623.78<br>AE 20620.77<br>EA          |                         |                         |                                                      |
|                             |                                                                | -2.97                   | -3.07                   | 0.10                                                 |                             |                                                                | -2.99                   | -3.28                   | 0.29                                                 |
|                             |                                                                | -5.77                   | -6.07                   | 0.30                                                 |                             |                                                                | -6.00                   | -6.67                   | 0.67                                                 |
|                             |                                                                | -                       | -6.36                   | -                                                    |                             |                                                                | -6.00                   | -6.62                   | 0.62                                                 |
| $1_{01} - 1_{10}$           | $2_1$ AA 18951.06<br>EE 18946.28<br>AE 18941.24<br>EA 18941.76 |                         |                         |                                                      | $2_{12} - 3_{03}$           | $2_1$ AA 24973.62<br>EE 24977.81<br>AE 24981.94<br>EA 24982.08 |                         |                         |                                                      |
|                             |                                                                | -4.78                   | -4.79                   | 0.02                                                 |                             |                                                                | 4.19                    | 4.26                    | -0.07                                                |
|                             |                                                                | -9.82                   | -9.96                   | 0.14                                                 |                             |                                                                | 8.31                    | 8.40                    | -0.09                                                |
|                             |                                                                | -9.30                   | -9.23                   | -0.08                                                |                             |                                                                | 8.46                    | 8.64                    | -0.18                                                |
|                             | $2_2$ AA 18921.05<br>EE 18912.92<br>AE 18904.02<br>EA 18905.59 |                         |                         |                                                      |                             | $2_2$ AA 24936.96<br>EE 24944.36<br>AE 24951.46<br>EA 24951.99 |                         |                         |                                                      |
|                             |                                                                | -8.13                   | -7.77                   | -0.36                                                |                             |                                                                | 7.40                    | 6.95                    | 0.45                                                 |
|                             |                                                                | -17.03                  | -16.44                  | -0.59                                                |                             |                                                                | 14.50                   | 13.64                   | 0.86                                                 |
|                             |                                                                | -15.46                  | -14.79                  | -0.68                                                |                             |                                                                | 15.03                   | 14.27                   | 0.76                                                 |
|                             | $2_3$ AA 18945.12<br>EE 18942.28<br>AE 18939.43<br>EA 18939.55 |                         |                         |                                                      |                             | $2_3$ AA 24891.12<br>EE 24893.58<br>AE 24896.04<br>EA          |                         |                         |                                                      |
|                             |                                                                | -2.85                   | -2.93                   | 0.08                                                 |                             |                                                                | 2.46                    | 2.50                    | -0.04                                                |
|                             |                                                                | -5.70                   | -6.09                   | 0.39                                                 |                             |                                                                | 4.92                    | 5.04                    | -0.12                                                |
|                             |                                                                | -5.58                   | -5.80                   | 0.22                                                 |                             |                                                                |                         | 5.14                    | -0.22                                                |
| $1_{11} - 2_{02}$           | $2_1$ AA 10149.87<br>EE 10154.38<br>AE 10159.10<br>EA          |                         |                         |                                                      | $4_{04} - 4_{13}$           | $2_1$ AA 22219.02<br>EE 22213.65<br>AE 22208.30<br>EA          |                         |                         |                                                      |
|                             |                                                                | 4.51                    | 4.69                    | -0.18                                                |                             |                                                                | -5.37                   | -5.76                   | 0.39                                                 |
|                             |                                                                | 9.23                    | 9.01                    | 0.22                                                 |                             |                                                                | -10.72                  | -11.54                  | 0.82                                                 |
|                             |                                                                | -                       | 9.76                    | -                                                    |                             |                                                                | -10.72                  | -11.51                  | 0.79                                                 |
|                             | $2_2$ AA 10139.39<br>EE 10147.35<br>AE<br>EA                   |                         |                         |                                                      |                             | $2_2$ AA 22090.70<br>EE 22081.41<br>AE 22072.13<br>EA          |                         |                         |                                                      |
|                             |                                                                | 7.96                    | 7.78                    | 0.18                                                 |                             |                                                                | -9.28                   | -9.58                   | 0.30                                                 |
|                             |                                                                | -                       | 14.74                   | -                                                    |                             |                                                                | -18.56                  | -19.28                  | 0.72                                                 |
|                             |                                                                | -                       | 16.51                   | -                                                    |                             |                                                                | -18.56                  | -19.20                  | 0.64                                                 |
|                             | $2_3$ AA 10103.53<br>EE 10106.33<br>AE 10108.89<br>EA          |                         |                         |                                                      |                             | $2_3$ AA 22045.72<br>EE 22042.59<br>AE 22039.46<br>EA          |                         |                         |                                                      |
|                             |                                                                | 2.80                    | 2.76                    | 0.04                                                 |                             |                                                                | -3.13                   | -3.54                   | 0.41                                                 |
|                             |                                                                | 5.36                    | 5.45                    | -0.09                                                |                             |                                                                | -6.26                   | -7.16                   | 0.90                                                 |
|                             |                                                                | -                       | 5.74                    | -                                                    |                             |                                                                | -6.26                   | -7.14                   | 0.88                                                 |
| $2_{02} - 2_{11}$           | $2_1$ AA 19645.53<br>EE 19640.57<br>AE 19635.54<br>EA 19635.68 |                         |                         |                                                      | $5_{05} - 5_{14}$           | $2_1$ AA 24189.13<br>EE 24183.48<br>AE 24177.82<br>EA          |                         |                         |                                                      |
|                             |                                                                | -4.97                   | -5.09                   | 0.12                                                 |                             |                                                                | -5.65                   | -6.24                   | 0.59                                                 |
|                             |                                                                | -9.99                   | -10.30                  | 0.31                                                 |                             |                                                                | -11.31                  | -12.49                  | 1.18                                                 |
|                             |                                                                | -9.85                   | -10.07                  | 0.22                                                 |                             |                                                                | -11.31                  | -12.50                  | 1.19                                                 |
|                             | $2_2$ AA 19595.44<br>EE 19586.82<br>AE 19578.06<br>EA 19578.58 |                         |                         |                                                      |                             | $2_2$ AA 23998.02<br>EE 23988.23<br>AE 23978.43<br>EA          |                         |                         |                                                      |
|                             |                                                                | -8.62                   | -8.36                   | -0.27                                                |                             |                                                                | -9.79                   | -10.45                  | 0.66                                                 |
|                             |                                                                | -17.38                  | -17.04                  | -0.34                                                |                             |                                                                | -19.59                  | -21.00                  | 1.41                                                 |
|                             |                                                                | -16.86                  | -16.54                  | -0.33                                                |                             |                                                                | -19.59                  | -20.99                  | 1.40                                                 |
|                             | $2_3$ AA 19605.38<br>EE 19602.46<br>AE 19599.54<br>EA          |                         |                         |                                                      |                             | $2_3$ AA 23908.70<br>EE 23905.40<br>AE 23902.12<br>EA          |                         |                         |                                                      |
|                             |                                                                | -2.92                   | -3.09                   | 0.17                                                 |                             |                                                                | -3.30                   | -3.86                   | 0.56                                                 |
|                             |                                                                | -5.84                   | -6.32                   | 0.48                                                 |                             |                                                                | -6.58                   | -7.81                   | 1.23                                                 |
|                             |                                                                | -5.84                   | -6.22                   | 0.38                                                 |                             |                                                                | -6.58                   | -7.80                   | 1.22                                                 |

Table 3 (continued).

| $J_{K-K_+}$<br>— $J_{K-K_+}$ | $\tilde{\nu}_n \Gamma \Gamma' \nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ | $J_{K-K_+}$<br>— $J_{K-K_+}$ | $\tilde{\nu}_n \Gamma \Gamma' \nu_{\text{exp}}$ | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ |
|------------------------------|-------------------------------------------------|---------------------------|---------------------------|----------------------------------------------------------|------------------------------|-------------------------------------------------|---------------------------|---------------------------|----------------------------------------------------------|
| $4_{23} - 5_{44}$            | $2_1$ AA 20221.96                               |                           |                           |                                                          | $5_{23} - 6_{16}$            | $2_3$ AA 21868.51                               |                           |                           |                                                          |
|                              | EE 20233.49                                     | 11.53                     | 14.60                     | -3.07                                                    |                              | EE 21876.04                                     | 7.53                      | 9.20                      | -1.67                                                    |
|                              | AE 20243.47                                     | 21.51                     | 25.40                     | -3.89                                                    |                              | AE 21883.74                                     | 15.22                     | 19.29                     | -4.07                                                    |
|                              | EA 20247.05                                     | 25.09                     | 32.70                     | -7.61                                                    |                              | EA 21883.22                                     | 14.71                     | 17.97                     | -3.26                                                    |
|                              | $2_2$ AA 20093.56                               |                           |                           |                                                          |                              | $6_{06} - 6_{15}$ $2_1$ AA 26690.32             |                           |                           |                                                          |
|                              | EE 20115.00                                     | 21.44                     | 24.90                     | -3.46                                                    |                              | EE 26684.29                                     | -6.03                     | -6.85                     | 0.82                                                     |
|                              | AE 20131.21                                     | 37.65                     | 41.30                     | -3.65                                                    |                              | AE 26678.24                                     | -12.08                    | -13.69                    | 1.61                                                     |
|                              | EA 20141.26                                     | 47.70                     | 58.00                     | -10.30                                                   |                              | EA                                              |                           | -13.74                    | 1.65                                                     |
|                              | $2_3$ AA 19904.61                               |                           |                           |                                                          |                              | $2_2$ AA 26416.94                               |                           |                           |                                                          |
|                              | EE 19910.53                                     | 5.92                      | 8.25                      | -2.33                                                    |                              | EE 26406.51                                     | -10.43                    | -11.56                    | 1.13                                                     |
|                              | AE 19916.58                                     | 11.97                     | 15.25                     | -3.28                                                    |                              | AE 26396.08                                     | -20.86                    | -23.19                    | 2.33                                                     |
|                              | EA                                              |                           | 18.28                     | -6.31                                                    |                              | EA                                              |                           | -23.22                    | 2.36                                                     |
| $5_{23} - 6_{16}$            | $2_1$ AA 21544.57                               |                           |                           |                                                          |                              | $2_3$ AA 26269.39                               |                           |                           |                                                          |
|                              | EE 21557.22                                     | 12.65                     | 14.87                     | -2.22                                                    |                              | EE 26265.90                                     | -3.48                     | -4.28                     | 0.80                                                     |
|                              | AE 21570.55                                     | 25.98                     | 31.36                     | -5.38                                                    |                              | AE 26262.42                                     | -6.97                     | -8.64                     | 1.67                                                     |
|                              | EA 21569.24                                     | 24.67                     | 28.18                     | -3.51                                                    |                              | EA                                              |                           | -8.64                     | 1.67                                                     |
|                              | $2_2$ AA 21787.37                               |                           |                           |                                                          |                              |                                                 |                           |                           |                                                          |
|                              | EE 21808.89                                     | 21.52                     | 24.04                     | -2.52                                                    |                              |                                                 |                           |                           |                                                          |
|                              | AE 21832.57                                     | 45.20                     | 52.03                     | -6.83                                                    |                              |                                                 |                           |                           |                                                          |
|                              | EA 21828.31                                     | 40.94                     | 44.65                     | -3.71                                                    |                              |                                                 |                           |                           |                                                          |
|                              |                                                 |                           |                           |                                                          |                              |                                                 |                           |                           |                                                          |
|                              |                                                 |                           |                           |                                                          |                              |                                                 |                           |                           |                                                          |
|                              |                                                 |                           |                           |                                                          |                              |                                                 |                           |                           |                                                          |
|                              |                                                 |                           |                           |                                                          |                              |                                                 |                           |                           |                                                          |

$\lambda_{gi}$  direction cosine between axis of top  $i$  and principal inertia axis  $g$ ,

$P_g$   $g$ -component of total angular momentum,

$p_i$  total angular momentum of top  $i$  along its symmetry-axis.

$$\mathcal{P}_i = \sum_g \lambda_{gi} I_\alpha P_g / I_g, \quad i = 1, 2;$$

$$F = \frac{\hbar}{4\pi} \frac{I_\alpha \left(1 - \sum_g \lambda_{gi}^2 I_\alpha / I_g\right)}{N},$$

$$F' = \frac{\hbar}{4\pi} \frac{I_\alpha^2 \sum_g \lambda_{g1} \lambda_{g2} / I_g}{N},$$

$$N = I_\alpha^2 \left(1 - \sum_g \lambda_{g1}^2 I_\alpha / I_g\right) \left(1 - \sum_g \lambda_{g2}^2 I_\alpha / I_g\right) - \left(\sum_g \lambda_{g1} \lambda_{g2} I_\alpha^2 / I_g\right)^2.$$

Discussions of the model and Hamiltonian may be found in Refs. [2–8], [11], [21].

Computer programs MELITA and MELISA originally written by Trinkaus [11, 22] and modified by Tan [23] were adapted to the Digital PDP 10 and TR 440.

Because of the size of the program overlay technique has to be used. Both programs use van

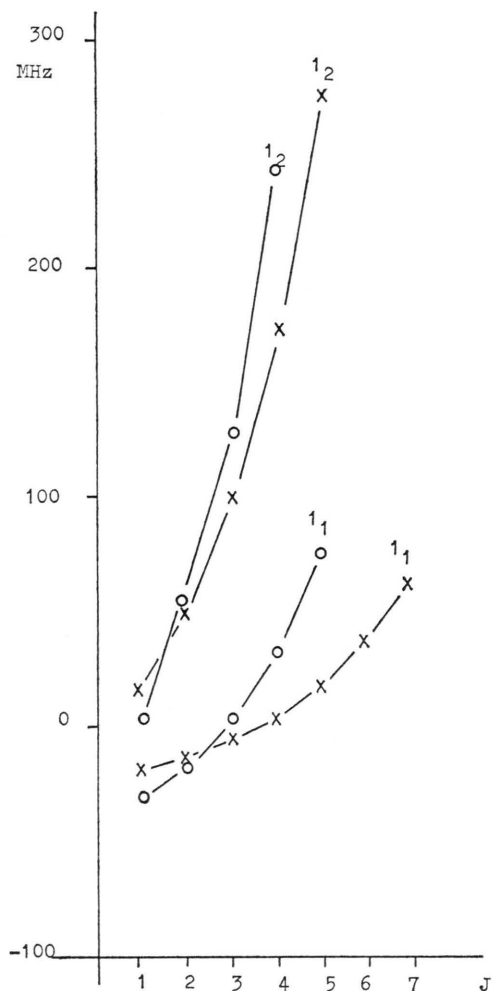
Vleck perturbation for the torsional levels and diagonalisation of the effective rotational matrix. In MELISA denominator correction is included. Details are given in [11, 18].

Trial calculations for (CH<sub>3</sub>)<sub>2</sub>O showed, that a basis set of uncoupled Mathieu functions for the two internal rotors with  $v_{\text{max}} = v_1 + v_2 = 8^*$  is sufficient [18]. In the worst case the calculated splittings for  $2_n$ -states changed by 2.2% using an extended basis set with  $v_{\text{max}} = 9$ , which is less than the error of the fitted splittings (see Table 10).

For (CD<sub>3</sub>)<sub>2</sub>O we observed difficulties in the convergence of the eigenvalues when  $v_{\text{max}}$  is varied. Limited by the computer size, we used  $v_{\text{max}} = 9$ . Similar observations were made by Durig et al. [13]. This fact implicates that the results for (CD<sub>3</sub>)<sub>2</sub>O are less reliable.

We investigated the dependence of the splittings on the potential parameters  $V_3$ ,  $V_{12}$ ,  $V'_{12}$  on the angle  $\angle(b, i)$  between the  $b$ - and internal rotation axis and the rotational constants  $A$ ,  $B$  and  $C$ . Table 9 characterises this dependence by a quadratic mean of partial derivatives QMPD( $X$ ) defined by:

\*  $v_i$  is the torsional quantum number of the Mathieu function.



◀ Fig. 1. Plot of the frequency shifts  $\nu_{O_1}^{A_1 A_1} - \nu_{\tilde{v}_n}^{A_1 A_1}$  ( $\tilde{v}_n = 1_1, 1_2$ ) as function of the rotational quantum number  $J$  of the series  $J_{0,J} - J_{1,J-1}$ . —○—  $(CH_3)_2O$ ; —×—  $(CD_3)_2O$ .

Table 4. Effective rotational constants and moments of inertia of  $(CD_3)_2O$  in torsional excited states.

| $\tilde{v}_n$      | $A, B, C$<br>MHz    | $I_g^c$<br>amu Å <sup>2</sup> | $\Delta^{b,c}$<br>amu Å <sup>2</sup> |
|--------------------|---------------------|-------------------------------|--------------------------------------|
| $0_1$ <sup>a</sup> | $A$ 25696.17 ± 0.11 | $I_a$ 19.67340                | 12.85897                             |
|                    | $B$ 7483.79 ± 0.03  | $I_b$ 67.55013                |                                      |
|                    | $C$ 6798.01 ± 0.06  | $I_c$ 74.36456                |                                      |
| $1_1$ $A_1 A_2$    | $A$ 25701.73 ± 0.09 | $I_a$ 19.66914                | 12.87164                             |
|                    | $B$ 7466.97 ± 0.03  | $I_b$ 67.70229                |                                      |
|                    | $C$ 6785.67 ± 0.05  | $I_c$ 74.49979                |                                      |
| $1_2$ $A_2 A_1$    | $A$ 25674.80 ± 0.09 | $I_a$ 19.68977                | 13.14617                             |
|                    | $B$ 7448.76 ± 0.03  | $I_b$ 67.86781                |                                      |
|                    | $C$ 6793.73 ± 0.05  | $I_c$ 74.41141                |                                      |
| $2_1$ $A_1 A_1$    | $A$ 25723.78 ± 0.08 | $I_a$ 19.65228                | 12.87801                             |
|                    | $B$ 7448.79 ± 0.02  | $I_b$ 67.86753                |                                      |
|                    | $C$ 6772.76 ± 0.03  | $I_c$ 74.64180                |                                      |
| $2_2$ $A_2 A_2$    | $A$ 25697.70 ± 0.08 | $I_a$ 19.67223                | 13.07997                             |
|                    | $B$ 7433.62 ± 0.02  | $I_b$ 68.00603                |                                      |
|                    | $C$ 6776.71 ± 0.03  | $I_c$ 74.59829                |                                      |
| $2_3$ $A_1 A_1$    | $A$ 25728.74 ± 0.06 | $I_a$ 19.64849                | 13.19140                             |
|                    | $B$ 7427.18 ± 0.02  | $I_b$ 68.06499                |                                      |
|                    | $C$ 6783.64 ± 0.02  | $I_c$ 74.52209                |                                      |
| $2_1$ $A_1 E$      | $A$ 25713.98 ± 0.15 | $I_a$ 19.65977                | 12.88734                             |
|                    | $B$ 7448.54 ± 0.04  | $I_b$ 67.86981                |                                      |
|                    | $C$ 6772.72 ± 0.05  | $I_c$ 74.64224                |                                      |
| $2_2$ $A_2 E$      | $A$ 25680.67 ± 0.07 | $I_a$ 19.68527                | 13.09610                             |
|                    | $B$ 7433.15 ± 0.02  | $I_b$ 68.01033                |                                      |
|                    | $C$ 6776.60 ± 0.02  | $I_c$ 74.59950                |                                      |
| $2_3$ $A_1 E$      | $A$ 25723.00 ± 0.09 | $I_a$ 19.65288                | 13.19686                             |
|                    | $B$ 7427.04 ± 0.02  | $I_b$ 68.06628                |                                      |
|                    | $C$ 6783.62 ± 0.03  | $I_c$ 74.52231                |                                      |

Errors are twice the standard errors.

<sup>a</sup> Lines not split in ground state.

<sup>b</sup>  $\Delta = I_a + I_b - I_c$ .

<sup>c</sup> Conversion factor 505 531 amu Å<sup>2</sup> MHz.

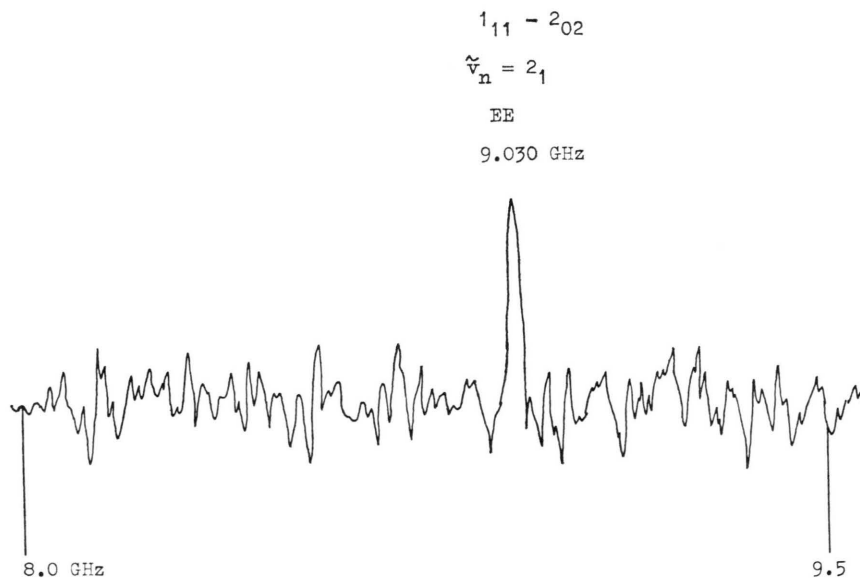


Fig. 3. Recording of a MW-MW-Douple resonance experiment. Signalfrequency 31 584.7 MHz EE component of  $2_{02} - 2_{11}$ ,  $\tilde{v}_n = 2_1$ . Pumpfrequency swept unstabilised from 8.5 to 9.5 in 3 min.

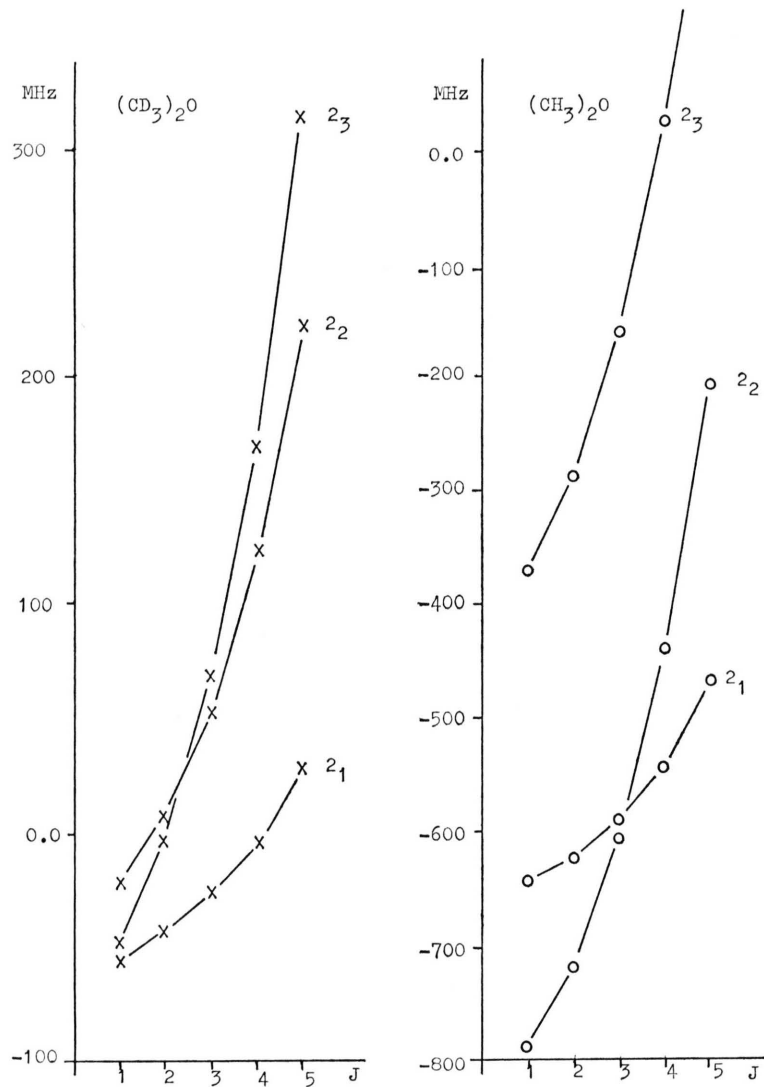


Fig. 2. Plot of the frequency shifts  $\nu_{01}^{A_1 A_1} - \nu_{\tilde{\nu}_n}^{A_1 A_2}$  ( $\tilde{\nu}_n = 2_1, 2_2, 2_3$ ) as function of the rotational quantum number  $J$  of the series  $J_{0,J} - J_{1,J-1}$ .

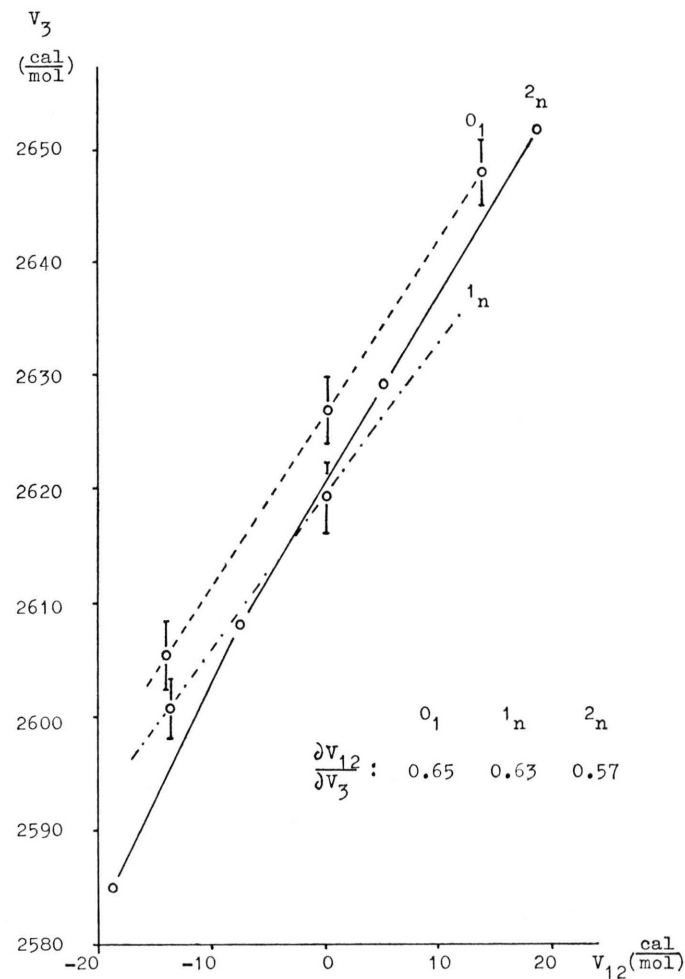


Fig. 4. Correlation of the potential parameters  $V_3$  and  $V_{12}$  for the states  $\tilde{\nu}_n = 0_1, 1_n, 2_n$  of  $(\text{CH}_3)_2\text{O}$  ( $F = 204.20$  GHz,  $F' = -40.91$  GHz,  $I_\alpha = 3.2084$  amu  $\text{\AA}^2$ ).

Table 5. Rotational lines of (CH<sub>3</sub>)<sub>2</sub>O for the  $\tilde{\nu}_n = 0_1$  torsional state [MHz].

| $J_{K-K+}$<br>$-J_{K'-K'+}$ | $\tilde{\nu}_n$ $\Gamma\Gamma'$ | $\nu_{\text{exp}}$                             | $\Delta\nu_{\text{exp}}$ | $\Delta\nu_{\text{cal}}$ | $\Delta\nu_{\text{exp}}$<br>$-\Delta\nu_{\text{cal}}$ |
|-----------------------------|---------------------------------|------------------------------------------------|--------------------------|--------------------------|-------------------------------------------------------|
| $1_{01} - 1_{10}$           | $0_1$ $A_1A_1$                  | 29902.29                                       |                          |                          |                                                       |
|                             | EE                              | 29901.40                                       | -0.89                    | -0.82                    | -0.07                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 29900.48                                       | -1.81                    | -1.69<br>-1.66           | -0.12<br>-0.15                                        |
| $1_{11} - 2_{02}$           | $0_1$ $A_1A_1$                  | 9118.82 <sup>a</sup>                           |                          |                          |                                                       |
|                             | EE                              | 9119.67 <sup>a</sup>                           | 0.85                     | 0.76                     | 0.09                                                  |
|                             | $A_1E$<br>EA <sub>1</sub>       | 9120.52 <sup>a</sup>                           | 1.70                     | 1.55<br>1.55             | 0.15<br>0.15                                          |
| $2_{02} - 2_{11}$           | $0_1$ $A_1A_1$                  | 31107.12                                       |                          |                          |                                                       |
|                             | EE                              | 31106.20                                       | -0.92                    | -0.85                    | -0.07                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 31105.26                                       | -1.86                    | -1.74<br>-1.72           | -0.12<br>-0.14                                        |
| $2_{21} - 3_{12}$           | $0_1$ $A_1A_1$                  | 27632.30                                       |                          |                          |                                                       |
|                             | EE                              | 27629.43                                       | -2.87                    | -2.88                    | 0.02                                                  |
|                             | $A_1E$<br>EA <sub>1</sub>       | 27627.56<br>27625.76                           | -4.74<br>-6.54           | -4.72<br>-6.87           | -0.02<br>0.33                                         |
| $2_{12} - 3_{03}$           | $0_1$ $A_1A_1$                  | 29091.33                                       |                          |                          |                                                       |
|                             | EE                              | 29092.12                                       | 0.79                     | 0.72                     | 0.07                                                  |
|                             | $A_1E$<br>EA <sub>1</sub>       | 29092.92                                       | 1.59                     | 1.46<br>1.45             | 0.13<br>0.12                                          |
| $3_{13} - 2_{20}$           | $0_1$ $A_1A_1$                  | 34684.63 <sup>a</sup>                          |                          |                          |                                                       |
|                             | EE                              | 34682.59 <sup>a</sup>                          | -2.04                    | -1.88                    | -0.16                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 34679.60 <sup>a</sup><br>34681.45 <sup>a</sup> | -5.03<br>-3.18           | -5.00<br>-2.76           | -0.03<br>-0.42                                        |
| $3_{03} - 3_{12}$           | $0_1$ $A_1A_1$                  | 32979.24                                       |                          |                          |                                                       |
|                             | EE                              | 32978.29                                       | -0.95                    | -0.89                    | -0.07                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 32977.34                                       | -1.90                    | -1.81<br>-1.79           | -0.09<br>-0.11                                        |
| $4_{04} - 4_{13}$           | $0_1$ $A_1A_1$                  | 35594.39                                       |                          |                          |                                                       |
|                             | EE                              | 35593.41                                       | -0.98                    | -0.94                    | -0.05                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 35592.40                                       | -1.99                    | -1.91<br>-1.90           | -0.08<br>-0.09                                        |
| $5_{05} - 5_{14}$           | $0_1$ $A_1A_1$                  | 39048.33                                       |                          |                          |                                                       |
|                             | EE                              | 39047.26                                       | -1.07                    | -1.01                    | -0.07                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 39046.26                                       | -2.07                    | -2.04<br>-2.03           | -0.03<br>-0.04                                        |
| $5_{24} - 6_{15}$           | $0_1$ $A_1A_1$                  | 37533.69                                       |                          |                          |                                                       |
|                             | EE                              | 37535.80                                       | 2.11                     | 2.09                     | 0.02                                                  |
|                             | $A_1E$<br>EA <sub>1</sub>       | 37537.92                                       | 4.23                     | 4.24<br>4.26             | -0.01<br>-0.03                                        |
| $6_{25} - 5_{32}^b$         | $0_1$ $A_1A_1$                  | 33399.68 <sup>a</sup>                          |                          |                          |                                                       |
|                             | EE                              | 33397.49 <sup>a</sup>                          | -2.19                    | -1.70                    | -0.49                                                 |
|                             | $A_1E$<br>EA <sub>1</sub>       | 33392.76 <sup>a</sup><br>33397.15 <sup>a</sup> | -6.92<br>-2.53           | -8.06<br>-0.75           | 1.14<br>-1.78                                         |

<sup>a</sup> Frequencies measured in this work; the other lines are from Ref. [19, 20].

<sup>b</sup> Not used for torsional analysis second order perturbation theory not sufficient.

$$\text{QMPD}(X) = \sqrt{\frac{1}{n} \sum_i^n \left( \frac{\partial \Delta\nu_i}{\partial X} \right)^2} \quad (3)$$

$n$  number of used splittings,

$\Delta\nu_i$  multiplet splitting,

$X, V_3, V_{12}, V'_{12}, \angle(b, i), A, B, C$ .

It may be observed that there is a noticeable dependence of the  $1_n$ -splittings on  $V'_{12}$  and of the  $2_n$ -splittings on  $V_{12}$  for both molecules.

In Table 10 we present sets of parameters which were fitted to the torsional fine structure of the rotational lines in the states  $\tilde{\nu}_n$ . These sets we consider as the final ones of the analysis. They resulted from many attempts described in more detail in [18]. The rotational constants were chosen from the respective fits to the ground state spectra (see Tables 4 and 8), as their variation was nearly without influence if the  $2_n$ -states of (CH<sub>3</sub>)<sub>2</sub>O are excepted. The fixed parameters are labelled by super  $f$ ,  $\angle(b, i) = 58.4^\circ$  results from the  $r_s$ -structure [19].  $I_\alpha$  was taken from [19]\*. Also  $V_{12}$  was fixed to  $V_{12} = 0$  after noticing, that there exists still a strong correlation to  $V_3$  also in the  $2_n$ -states. The dependence  $V_3 = f(V_{12})$  is given in Figure 4.

It must be noticed that for all  $\tilde{\nu}_n$ -states  $\partial V_{12}/\partial V_3$  is nearly equal so that even by combining all states no reliable value of  $V_{12}$  can be determined.

It was proposed [24] to chose another combination of potential parameters:  $V_3 - V_{12}$ ,  $V_3$  to improve the results. We could not proof it.

The sets of parameters of Table 10 were used to calculate  $\Delta\nu_{\text{calc}}$  of Tables 2, 3, 5–7. Only for the  $2_n$ -states of (CH<sub>3</sub>)<sub>2</sub>O we used a slightly modified set. Taking the values for  $s$ ,  $V_{12}$ ,  $V'_{12}$  as given for the  $2_n$ -states in the last column of Table 10 we fitted in addition the angle  $\angle(b, i)$  to  $59.5 \pm 0.6^\circ$ .  $\sigma_{\text{rel}}$  was reduced from 3.5% to 2.9%.

To compare our analysis with results of other authors [12, 13], we give in Table 11 results, which we gained under the assumptions made by these authors:  $A, B, C$  ground state values,  $V_{12} = 0$ ,  $\angle(b, i) = 58.4^\circ$ . Although the computational methods of [12, 13] were different from ours the agreement of the results is reasonable. For the  $\tilde{\nu}_n = 2_n$ -states of (CH<sub>3</sub>)<sub>2</sub>O no data could be found in the literature.

\* The conversion factor was corrected to 505.531 amu Å<sup>2</sup> · GHz.

Table 6. Rotational lines of (CH<sub>3</sub>)<sub>2</sub>O for the  $\tilde{\nu}_n = 1_1$  and  $1_2$  torsional states [MHz].

| $J_{K_-K_1}$<br>— $J_{K_-K_+}$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta\nu_{\text{exp}}$ | $\Delta\nu_{\text{cal}}$ | $\Delta\nu_{\text{exp}}$<br>— $\Delta\nu_{\text{cal}}$ | $J_{K_-K_1}$<br>— $J_{K_-K_+}$ | $\tilde{\nu}_n \Gamma \Gamma'$                    | $\nu_{\text{exp}}$ | $\Delta\nu_{\text{exp}}$ | $\Delta\nu_{\text{cal}}$ | $\Delta\nu_{\text{exp}}$<br>— $\Delta\nu_{\text{cal}}$ |
|--------------------------------|---------------------------------------------------|--------------------|--------------------------|--------------------------|--------------------------------------------------------|--------------------------------|---------------------------------------------------|--------------------|--------------------------|--------------------------|--------------------------------------------------------|
| $1_{01} - 1_{10}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 29929.98           |                          |                          |                                                        | $3_{03} - 3_{12}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 32973.40           |                          |                          |                                                        |
|                                |                                                   | 29957.06           | 27.08                    | 27.05                    | 0.04                                                   |                                |                                                   | 32999.11           | 25.71                    | 25.74                    | -0.03                                                  |
|                                |                                                   | 29977.93           | 47.98                    | 47.71                    | 0.27                                                   |                                |                                                   | 33023.84           | 50.44                    | 50.48                    | -0.04                                                  |
|                                |                                                   | 29990.26           | 60.28                    | 60.39                    | -0.11                                                  |                                |                                                   | 33025.77           | 52.37                    | 52.52                    | -0.15                                                  |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 29900.28           |                          |                          |                                                        |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 32848.29           |                          |                          |                                                        |
|                                |                                                   | 29926.22           | 25.94                    | 25.85                    | 0.09                                                   |                                |                                                   | 32872.88           | 24.61                    | 24.67                    | -0.06                                                  |
|                                |                                                   | 29946.15           | 45.88                    | 45.68                    | 0.19                                                   |                                |                                                   | 32896.52           | 48.23                    | 48.36                    | -0.13                                                  |
|                                |                                                   | 29958.05           | 57.78                    | 57.59                    | 0.19                                                   |                                |                                                   | 32898.40           | 50.11                    | 50.28                    | -0.17                                                  |
|                                | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 31121.93           |                          |                          |                                                        |                                | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 35558.53           |                          |                          |                                                        |
|                                |                                                   | 31147.43           | 25.50                    | 25.45                    | 0.05                                                   |                                |                                                   | 35585.05           | 26.53                    | 26.63                    | -0.10                                                  |
|                                |                                                   | 31170.86           | 48.93                    | 48.82                    | 0.11                                                   |                                |                                                   | 35611.02           | 52.50                    | 52.71                    | -0.21                                                  |
|                                |                                                   | 31174.94           | 53.01                    | 53.03                    | -0.02                                                  |                                |                                                   | 35612.06           | 53.54                    | 53.87                    | -0.33                                                  |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 31055.55           |                          |                          |                                                        |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 35348.40           |                          |                          |                                                        |
|                                |                                                   | 31079.95           | 24.39                    | 24.38                    | 0.01                                                   |                                |                                                   | 35373.75           | 25.34                    | 25.54                    | -0.20                                                  |
|                                |                                                   | 31102.35           | 46.80                    | 46.75                    | 0.05                                                   |                                |                                                   | 35398.54           | 50.14                    | 50.52                    | -0.38                                                  |
|                                |                                                   | -                  | -                        | -                        | -                                                      |                                |                                                   | 35399.57           | 51.17                    | 51.60                    | -0.43                                                  |
| $1_{11} - 2_{02}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 8978.34            |                          |                          |                                                        | $5_{05} - 5_{14}$              | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 38971.06           |                          |                          |                                                        |
|                                |                                                   | 8959.12            | -19.21                   | -19.10                   | -0.11                                                  |                                |                                                   | 38998.75           | 27.69                    | 27.93                    | -0.24                                                  |
|                                |                                                   | 8933.67            | -44.67                   | -44.67                   | 0.00                                                   |                                |                                                   | 39026.14           | 55.08                    | 55.54                    | -0.46                                                  |
|                                |                                                   | 8946.03            | -32.30                   | -31.90                   | -0.40                                                  |                                |                                                   | 39026.73           | 55.67                    | 56.25                    | -0.42                                                  |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 8917.19            |                          |                          |                                                        |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 38644.50           |                          |                          |                                                        |
|                                |                                                   | 8898.79            | -18.40                   | -18.40                   | 0.00                                                   |                                |                                                   | 38670.95           | 26.45                    | 26.81                    | -0.36                                                  |
|                                |                                                   | 8874.39            | -42.80                   | -42.75                   | -0.05                                                  |                                |                                                   | 38697.07           | 52.57                    | 53.26                    | -0.31                                                  |
|                                |                                                   | 8886.42            | -30.77                   | -30.80                   | -0.03                                                  |                                |                                                   | 38697.67           | 53.17                    | 53.91                    | -0.74                                                  |
|                                | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 28890.84           |                          |                          |                                                        |                                | $1_1 A_1 A_2$<br>EE<br>$A_1 E$<br>EA <sub>2</sub> | 14863.06           |                          |                          |                                                        |
|                                |                                                   | 28870.72           | -20.12                   | -20.23                   | 0.10                                                   |                                |                                                   | 14821.70           | -41.36                   | -36.35                   | -5.01                                                  |
|                                |                                                   | 28848.52           | -42.32                   | -42.67                   | 0.35                                                   |                                |                                                   | 14741.93           | -121.13                  | -128.51                  | 7.38                                                   |
|                                |                                                   | 28852.70           | -38.15                   | -38.30                   | 0.15                                                   |                                |                                                   | 14819.25           | -43.81                   | -30.00                   | -13.81                                                 |
|                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 28773.94           |                          |                          |                                                        |                                | $1_2 A_2 A_1$<br>EE<br>$A_2 E$<br>EA <sub>1</sub> | 14508.03           |                          |                          |                                                        |
|                                |                                                   | 28754.63           | -19.31                   | -19.42                   | 0.12                                                   |                                |                                                   | 14468.90           | -39.13                   | -35.22                   | -3.91                                                  |
|                                |                                                   | 28733.36           | -40.59                   | -40.82                   | 0.23                                                   |                                |                                                   | 14391.57           | -116.46                  | -122.95                  | 6.49                                                   |
|                                |                                                   | 28737.36           | -36.58                   | -36.76                   | 0.18                                                   |                                |                                                   | 14465.90           | -42.13                   | -29.15                   | -12.98                                                 |

## Discussion

It must be stated, that the potential coefficient  $V_{12}$  could not be determined in spite of many efforts. But  $V_3$  and  $V'_{12}$  are reliable values. It should be mentioned, that as in similar work only the splittings of the multiplets have been used in the analysis.

No decision can be made between the results of two quantum chemical calculations [25, 26] for  $V_{12}$  and  $V'_{12}$ .

As in similar molecules, there is a difference in the effective potential parameters for the CH<sub>3</sub>- and CD<sub>3</sub> isotopes [23, 27, 28].

Further work should include more experimental data. Highly resolved infrared and Raman bands would be of use. They are presently not available. The analysis should perhaps be based on a more general Hamiltonian, as there is an interaction of the  $\tilde{\nu}_n = 2_n$ -states to the COC-bending state, which we noticed from the rotational spectrum [18] in the first excited bending state.

For other molecules the situation may be more favourable, as for (CH<sub>3</sub>)<sub>2</sub>O  $F'$  dominates  $V_{12}$  and  $V'_{12}$  in the influence on the splittings. (CH<sub>3</sub>)<sub>2</sub>S may be a possible candidate.

Table 7. Rotational lines of (CH<sub>3</sub>)<sub>2</sub>O for the  $\tilde{\nu}_n = 2_1, 2_2$  and  $2_3$  torsional states [MHz], for  $\tilde{\nu}_n = 2_1$  and  $2_3$ : A<sub>1</sub>A<sub>1</sub>, EE, A<sub>1</sub>E, EA<sub>1</sub>, for  $\tilde{\nu}_n = 2_2$ : A<sub>2</sub>A<sub>2</sub>, EE, A<sub>2</sub>E, EA<sub>2</sub>.

| $J_{K-K_+}$<br>— $J_{K-K_+}'$ | $\tilde{\nu}_n \Gamma \Gamma' \nu_{\text{exp}}$                      | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ | $J_{K-K_+}$<br>— $J_{K-K_+}'$ | $\tilde{\nu}_n \Gamma \Gamma' \nu_{\text{exp}}$                | $\Delta \nu_{\text{exp}}$ | $\Delta \nu_{\text{cal}}$ | $\Delta \nu_{\text{exp}}$<br>— $\Delta \nu_{\text{cal}}$ |
|-------------------------------|----------------------------------------------------------------------|---------------------------|---------------------------|----------------------------------------------------------|-------------------------------|----------------------------------------------------------------|---------------------------|---------------------------|----------------------------------------------------------|
| $1_{01} - 1_{10}$             | $2_1$ AA 30543.46<br>EE 30653.48<br>AE 29878.13<br>EA — <sup>a</sup> |                           |                           |                                                          | $5_{05} - 5_{14}$             | $2_1$ AA 39521.11<br>EE 39189.63<br>AE 38794.23<br>EA 38914.16 |                           |                           |                                                          |
|                               |                                                                      | 110.02                    | 119.86                    | -9.84                                                    |                               |                                                                | -331.46                   | -329.95                   | -1.51                                                    |
|                               |                                                                      | -665.33                   | -646.60                   | -18.73                                                   |                               |                                                                | -726.88                   | -730.28                   | 3.40                                                     |
|                               |                                                                      | —                         | 564.70                    | —                                                        |                               |                                                                | -606.95                   | -597.78                   | -9.20                                                    |
|                               | $2_2$ AA 30691.47<br>EE 31094.93<br>AE 29634.61<br>EA —              |                           |                           |                                                          |                               | $2_2$ AA 39261.07<br>EE 38788.24<br>AE 38154.80<br>EA 38477.85 |                           |                           |                                                          |
|                               |                                                                      | 403.46                    | 422.84                    | -19.38                                                   |                               |                                                                | -472.83                   | -492.41                   | 19.58                                                    |
|                               |                                                                      | -1056.86                  | -1060.23                  | 3.37                                                     |                               |                                                                | -1106.27                  | -1160.99                  | 54.72                                                    |
|                               |                                                                      | —                         | —                         | —                                                        |                               |                                                                | -783.22                   | -802.05                   | 18.83                                                    |
|                               | $2_3$ AA 30279.18<br>EE 30276.88<br>AE 29928.78<br>EA —              |                           |                           |                                                          |                               | $2_3$ AA 38769.23<br>EE 38582.05<br>AE 38735.46<br>EA 38417.29 |                           |                           |                                                          |
|                               |                                                                      | -2.30                     | -5.77                     | 3.47                                                     |                               |                                                                | -187.18                   | -187.63                   | 0.45                                                     |
|                               |                                                                      | -350.40                   | -338.09                   | -12.31                                                   |                               |                                                                | -393.77                   | -390.34                   | -3.43                                                    |
|                               |                                                                      | —                         | 171.45                    | —                                                        |                               |                                                                | -351.94                   | -353.42                   | 1.48                                                     |
| $2_{02} - 2_{11}$             | $2_1$ AA 31729.03<br>EE 31584.75<br>AE 31057.96<br>EA — <sup>a</sup> |                           |                           |                                                          | $1_{11} - 2_{02}$             | $2_1$ AA 8283.53<br>EE 9030.36<br>AE —<br>EA —                 |                           |                           |                                                          |
|                               |                                                                      | -144.28                   | -134.28                   | -10.00                                                   |                               |                                                                | 746.83                    | 737.46                    | 9.37                                                     |
|                               |                                                                      | -671.07                   | -655.27                   | -15.80                                                   |                               |                                                                | —                         | 599.10                    | —                                                        |
|                               |                                                                      | —                         | 30.03                     | —                                                        |                               |                                                                | —                         | 1814.20                   | —                                                        |
|                               | $2_2$ AA 31827.14<br>EE 31787.16<br>AE 30770.16<br>EA 32297.64       |                           |                           |                                                          |                               | $2_2$ AA 8109.00<br>EE 9544.79<br>AE —<br>EA —                 |                           |                           |                                                          |
|                               |                                                                      | -39.98                    | -31.31                    | -8.68                                                    |                               |                                                                | 1435.79                   | 1454.12                   | -18.33                                                   |
|                               |                                                                      | -1056.98                  | -1066.16                  | 9.17                                                     |                               |                                                                | —                         | 979.59                    | —                                                        |
|                               |                                                                      | 470.50                    | 503.91                    | -33.41                                                   |                               |                                                                | —                         | 3318.28                   | —                                                        |
|                               | $2_3$ AA 31403.78<br>EE 31288.53<br>AE 31048.96<br>EA —              |                           |                           |                                                          |                               | $2_3$ AA 8383.20<br>EE —<br>AE —<br>EA —                       |                           |                           |                                                          |
|                               |                                                                      | -115.25                   | -113.06                   | -2.19                                                    |                               |                                                                | —                         | 325.48                    | —                                                        |
|                               |                                                                      | -354.82                   | -344.44                   | -10.38                                                   |                               |                                                                | —                         | 313.67                    | —                                                        |
|                               |                                                                      | —                         | -116.57                   | —                                                        |                               |                                                                | —                         | 831.25                    | —                                                        |
| $3_{03} - 3_{12}$             | $2_1$ AA 33569.01<br>EE 33324.29<br>AE 32887.36<br>EA 33254.43       |                           |                           |                                                          | $2_{12} - 3_{03}$             | $2_1$ AA 28158.87<br>EE 28638.56<br>AE 28739.27<br>EA —        |                           |                           |                                                          |
|                               |                                                                      | -244.72                   | -236.49                   | -8.24                                                    |                               |                                                                | 479.69                    | 473.32                    | 6.37                                                     |
|                               |                                                                      | -681.65                   | -670.54                   | -11.11                                                   |                               |                                                                | 580.40                    | 564.48                    | 15.93                                                    |
|                               |                                                                      | -314.58                   | -293.43                   | -21.15                                                   |                               |                                                                | —                         | 1265.41                   | —                                                        |
|                               | $2_2$ AA 33586.76<br>EE 33311.17<br>AE 32524.62<br>EA 33455.81       |                           |                           |                                                          |                               | $2_2$ AA 27958.78<br>EE 28921.73<br>AE 28872.13<br>EA —        |                           |                           |                                                          |
|                               |                                                                      | -275.59                   | -274.60                   | -0.99                                                    |                               |                                                                | 962.95                    | 979.55                    | -16.60                                                   |
|                               |                                                                      | -1062.14                  | -1080.93                  | 18.79                                                    |                               |                                                                | 913.35                    | 917.16                    | -3.81                                                    |
|                               |                                                                      | -130.95                   | -112.42                   | -18.53                                                   |                               |                                                                | —                         | 2556.25                   | —                                                        |
|                               | $2_3$ AA 33146.79<br>EE 32994.13<br>AE 32784.80<br>EA 32903.63       |                           |                           |                                                          |                               | $2_3$ AA 28154.74<br>EE 28380.54<br>AE 28465.07<br>EA —        |                           |                           |                                                          |
|                               |                                                                      | -152.66                   | -149.65                   | -3.01                                                    |                               |                                                                | 225.80                    | 213.66                    | 12.14                                                    |
|                               |                                                                      | -361.99                   | -354.71                   | -7.28                                                    |                               |                                                                | 310.33                    | 296.60                    | 13.73                                                    |
|                               |                                                                      | -243.16                   | -240.40                   | -2.76                                                    |                               |                                                                | —                         | 535.98                    | —                                                        |
| $4_{04} - 4_{13}$             | $2_1$ AA 36135.87<br>EE 35840.21<br>AE 35436.42<br>EA 35643.96       |                           |                           |                                                          |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -295.66                   | -290.33                   | -5.34                                                    |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -699.45                   | -694.72                   | -4.73                                                    |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -491.91                   | -475.79                   | -16.12                                                   |                               |                                                                |                           |                           |                                                          |
|                               | $2_2$ AA 36036.59<br>EE 35639.35<br>AE 34959.49<br>EA 35510.90       |                           |                           |                                                          |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -397.24                   | -404.75                   | 7.50                                                     |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -1077.10                  | -1110.47                  | 33.36                                                    |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -525.69                   | -523.57                   | -2.12                                                    |                               |                                                                |                           |                           |                                                          |
|                               | $2_3$ AA 35574.08<br>EE 35401.77<br>AE 35201.37<br>EA 35265.78       |                           |                           |                                                          |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -172.31                   | -170.43                   | -1.88                                                    |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -372.71                   | -369.71                   | -3.00                                                    |                               |                                                                |                           |                           |                                                          |
|                               |                                                                      | -308.30                   | -306.21                   | -2.09                                                    |                               |                                                                |                           |                           |                                                          |

<sup>a</sup> EA<sub>i</sub>-components could not be assigned unambiguously.

Table 8. Effective rotational constants and moments of inertia of (CH<sub>3</sub>)<sub>2</sub>O in torsional excited states.

| $\bar{\nu}_n$                                | $A, B, C$<br>MHz                                                             | $I_g^c$<br>amu Å <sup>2</sup>                      | $\Delta^{b,c}$<br>amu Å <sup>2</sup> |
|----------------------------------------------|------------------------------------------------------------------------------|----------------------------------------------------|--------------------------------------|
| 0 <sub>1</sub> A <sub>1</sub> A <sub>1</sub> | A 38788.46 <sup>a</sup><br>B 10056.48 <sup>a</sup><br>C 8886.87 <sup>a</sup> | $I_a$ 13.03303<br>$I_b$ 50.26918<br>$I_c$ 56.88516 | 6.417049                             |
| 1 <sub>1</sub> A <sub>1</sub> A <sub>2</sub> | A 38797.34 ± 0.30<br>B 10024.95 ± 0.05<br>C 8867.34 ± 0.10                   | $I_a$ 13.03004<br>$I_b$ 50.42728<br>$I_c$ 57.01045 | 6.446882                             |
| 1 <sub>2</sub> A <sub>2</sub> A <sub>1</sub> | A 38770.43 ± 0.30<br>B 9993.07 ± 0.05<br>C 8870.13 ± 0.10                    | $I_a$ 13.03909<br>$I_b$ 50.58816<br>$I_c$ 56.99249 | 6.634751                             |
| 2 <sub>1</sub> A <sub>1</sub> A <sub>1</sub> | A 39394.67 ± 0.44<br>B 10003.35 ± 0.09<br>C 8851.08 ± 0.13                   | $I_a$ 12.83247<br>$I_b$ 50.53617<br>$I_c$ 57.11518 | 6.253465                             |
| 2 <sub>2</sub> A <sub>2</sub> A <sub>2</sub> | A 39571.26 ± 0.17<br>B 9984.53 ± 0.04<br>C 8879.56 ± 0.05                    | $I_a$ 12.77521<br>$I_b$ 50.63143<br>$I_c$ 56.93199 | 6.474645                             |
| 2 <sub>3</sub> A <sub>1</sub> A <sub>1</sub> | A 39131.42 ± 0.32<br>B 9946.58 ± 0.06<br>C 8852.25 ± 0.09                    | $I_a$ 12.91880<br>$I_b$ 50.82461<br>$I_c$ 57.10763 | 6.63578                              |
| 1 <sub>1</sub> A <sub>1</sub> E              | A 38845.39 ± 0.23<br>B 10026.04 ± 0.04<br>C 8867.44 ± 0.08                   | $I_a$ 13.01393<br>$I_b$ 50.42180<br>$I_c$ 57.00980 | 6.425929                             |
| 1 <sub>2</sub> A <sub>2</sub> E              | A 38816.41 ± 0.23<br>B 9994.10 ± 0.04<br>C 8870.23 ± 0.08                    | $I_a$ 13.02364<br>$I_b$ 50.58294<br>$I_c$ 56.99187 | 6.614709                             |
| 2 <sub>1</sub> A <sub>1</sub> E              | A 38717.34 ± 3.29<br>B 9988.42 ± 0.70<br>C 8845.67 ± 0.99                    | $I_a$ 13.05360<br>$I_b$ 50.61171<br>$I_c$ 57.15011 | 6.515200                             |
| 2 <sub>2</sub> A <sub>2</sub> E              | A 38508.39 ± 7.76<br>B 9960.89 ± 1.65<br>C 8865.29 ± 2.34                    | $I_a$ 13.12781<br>$I_b$ 50.75159<br>$I_c$ 57.02363 | 6.855770                             |
| 2 <sub>3</sub> A <sub>1</sub> E              | A 38781.98 ± 2.58<br>B 9939.18 ± 0.55<br>C 8851.03 ± 0.78                    | $I_a$ 13.03520<br>$I_b$ 50.86245<br>$I_c$ 57.11550 | 6.782150                             |

Errors are twice the standard errors.

<sup>a</sup> See Ref. [19], <sup>b</sup> and <sup>c</sup> see Table 4.Table 9. Quadratic mean partial derivatives for the torsional states of (CH<sub>3</sub>)<sub>2</sub>O and (CD<sub>3</sub>)<sub>2</sub>O.

| $x$                     | (CH <sub>3</sub> ) <sub>2</sub> O |                |                | (CD <sub>3</sub> ) <sub>2</sub> O |                              |
|-------------------------|-----------------------------------|----------------|----------------|-----------------------------------|------------------------------|
|                         | 0 <sub>1</sub>                    | 1 <sub>n</sub> | 2 <sub>n</sub> | 1 <sub>n</sub>                    | 2 <sub>n</sub>               |
| $V_3$                   | 12                                | 98             | 1100           | 4                                 | 47 kHz/cal mol <sup>-1</sup> |
| $V_{12}$                | —                                 | —              | 1900           | —                                 | 64 kHz/cal mol <sup>-1</sup> |
| $V'_{12}$               | —                                 | 40             | 500            | 3                                 | 20 kHz/cal mol <sup>-1</sup> |
| $\sphericalangle(b, i)$ | 110                               | 280            | 5500           | 84                                | 490 kHz/Grad                 |
| $A$                     | —                                 | —              | 192            | —                                 | — kHz/MHz                    |
| $B$                     | —                                 | —              | 202            | —                                 | — kHz/MHz                    |
| $C$                     | —                                 | —              | 145            | —                                 | — kHz/MHz                    |

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Table 10. Results of the analysis of the torsional fine structure.

|                                          | (CD <sub>3</sub> ) <sub>2</sub> O |                     | (CH <sub>3</sub> ) <sub>2</sub> O |                     |                     |
|------------------------------------------|-----------------------------------|---------------------|-----------------------------------|---------------------|---------------------|
|                                          | 1 <sub>n</sub>                    | 2 <sub>n</sub>      | 0 <sub>1</sub>                    | 1 <sub>n</sub>      | 2 <sub>n</sub>      |
| $s$                                      | 103.39 ± 0.80                     | 103.14 ± 0.19       | 60.32 ± 0.16                      | 59.96 ± 0.02        | 59.76 ± 0.9         |
| $V_3$ [cal/mole]                         | 2584 ± 20                         | 2572 ± 6            | 2630 ± 7                          | 2663 ± 2            | 2618 ± 4            |
| $V_{12}$ [cal/mole]                      | 0.0 <sup>f</sup>                  | 0.0 <sup>f</sup>    | 0.0 <sup>f</sup>                  | 0.0 <sup>f</sup>    | 0.0 <sup>f</sup>    |
| $V'_{12}$ [cal/mole]                     | 21 ± 50                           | 29 ± 12             | 0.0 <sup>f</sup>                  | 13 ± 2              | 18 ± 8              |
| $\sphericalangle(b, i)$                  | 58.6 ± 2.0                        | 58.4 <sup>f</sup>   | 57.7 ± 8                          | 60.6 ± 0.2          | 58.4 <sup>f</sup>   |
| $F$ [GHz]                                | 116.51                            | 116.25              | 203.24                            | 207.02              | 204.20              |
| $F'$ [GHz]                               | -33.60                            | -33.28              | -39.7                             | -44.44              | -40.91              |
| $I_x$ [amu Å <sup>2</sup> ] <sup>a</sup> | 6.4294 <sup>f</sup>               | 6.4294 <sup>f</sup> | 3.2084 <sup>f</sup>               | 3.2084 <sup>f</sup> | 3.2084 <sup>f</sup> |
| $\sigma$ [MHz]                           | 0.07                              | 0.40                | 0.14                              | 0.19                | 16.46               |
| $\sigma$ [rel%]                          | 10.1                              | 4.5                 | 6.3                               | 0.5                 | 3.5                 |
|                                          | 1                                 | 1                   | 1                                 | 1                   | 1                   |
| Corr. C                                  | -0.6 1                            | -0.6 1              | -0.6 1                            | -0.4 1              | -0.2 1              |
|                                          | 0.3-0.9 1                         |                     |                                   | -0.6-0.2 1          |                     |

Errors are twice the standard errors.  $\sigma$  mean square deviation of the splittings,  $\sigma_{\text{rel}} = \left( \sigma / \frac{1}{n} \sum_{i=1}^n \Delta v_i \right) \cdot 100$ .

$\Delta v_i$  multiplett splitting,  $n$  number of lines. Corr. C Elements of the correlation matrix.

<sup>a</sup> Taken from [19] conversion factor changed to 505.531 amu Å<sup>2</sup> GHz. <sup>f</sup> parameter fixed.

Table 11. Comparison of the torsional parameters.

|                                             | (CD <sub>3</sub> ) <sub>2</sub> O |                     |                                      |                             | (CH <sub>3</sub> ) <sub>2</sub> O |                     |                                      |
|---------------------------------------------|-----------------------------------|---------------------|--------------------------------------|-----------------------------|-----------------------------------|---------------------|--------------------------------------|
|                                             | 1 <sub>n</sub> <sup>a</sup>       | 1 <sub>n</sub> [13] | 1 <sub>n</sub> + 2 <sub>n</sub> [12] | 2 <sub>n</sub> <sup>a</sup> | 1 <sub>n</sub> <sup>a</sup>       | 1 <sub>n</sub> [13] | 0 <sub>1</sub> + 1 <sub>n</sub> [12] |
| <i>s</i>                                    | 103.58 ± 0.05                     | — <sup>b</sup>      | — <sup>b</sup>                       | 103.14 ± 0.19               | 59.79 ± 0.06                      | — <sup>b</sup>      | — <sup>b</sup>                       |
| <i>V</i> <sub>3</sub> [cal/mole]            | 2583 ± 4                          | 2564.7              | 2580 ± 64                            | 2572 ± 6                    | 2619 ± 3                          | 2599 ± 1.4          | 2605 ± 14                            |
| <i>V</i> <sub>12</sub> [cal/mole]           | 0.0 <sup>f</sup>                  | 0.0 <sup>f</sup>    | 17 ± 17                              | 29 ± 12                     | 14 ± 7                            | 14.5 ± 4.6          | 17 ± 17                              |
| ϕ <sub>12</sub> ( <i>b</i> , <i>i</i> )     | 58.4                              | 58.4 <sup>f</sup>   | — <sup>b</sup>                       | 58.4 <sup>f</sup>           | 58.4 <sup>f</sup>                 | 58.4 <sup>f</sup>   | — <sup>b</sup>                       |
| <i>F</i> [GHz]                              | 116.25                            | 116.04 <sup>c</sup> | — <sup>b</sup>                       | 116.25                      | 204.20                            | 203.36              | — <sup>b</sup>                       |
| <i>F</i> ' [GHz]                            | —33.28                            | —33.37 <sup>c</sup> | — <sup>b</sup>                       | —33.28                      | —40.91                            | —41.09              | — <sup>b</sup>                       |
| <i>I</i> <sub>α</sub> [amu Å <sup>2</sup> ] | 6.4294 <sup>f</sup>               | 6.4511 <sup>f</sup> | — <sup>b</sup>                       | 6.4294 <sup>f</sup>         | 3.2084 <sup>f</sup>               | 3.2282 <sup>f</sup> | — <sup>b</sup>                       |

Assumed *V*<sub>12</sub> = 0, rotational constants from ground state, <sup>a</sup> this work, <sup>b</sup> no data given, <sup>c</sup> mean value of Table 7 of [13], <sup>f</sup> parameter fixed.

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